



Reconstruction of Radio Interferometric Images

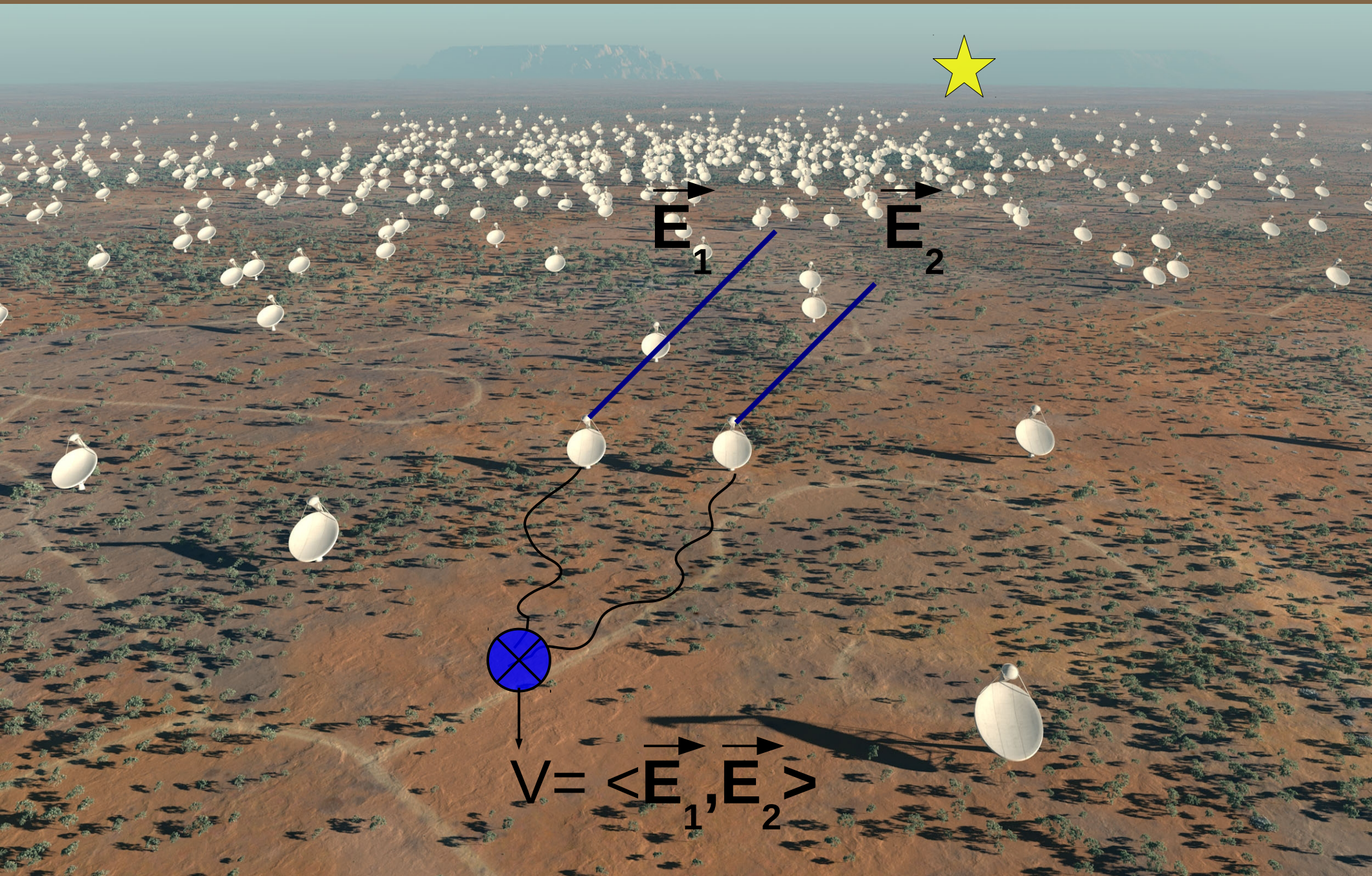
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PhD Supervisors: Chiara Ferrari, Eric Slezak (OCA)

With the collaboration of: David Mary (OCA), Oleg Smirnov (SKA SA)

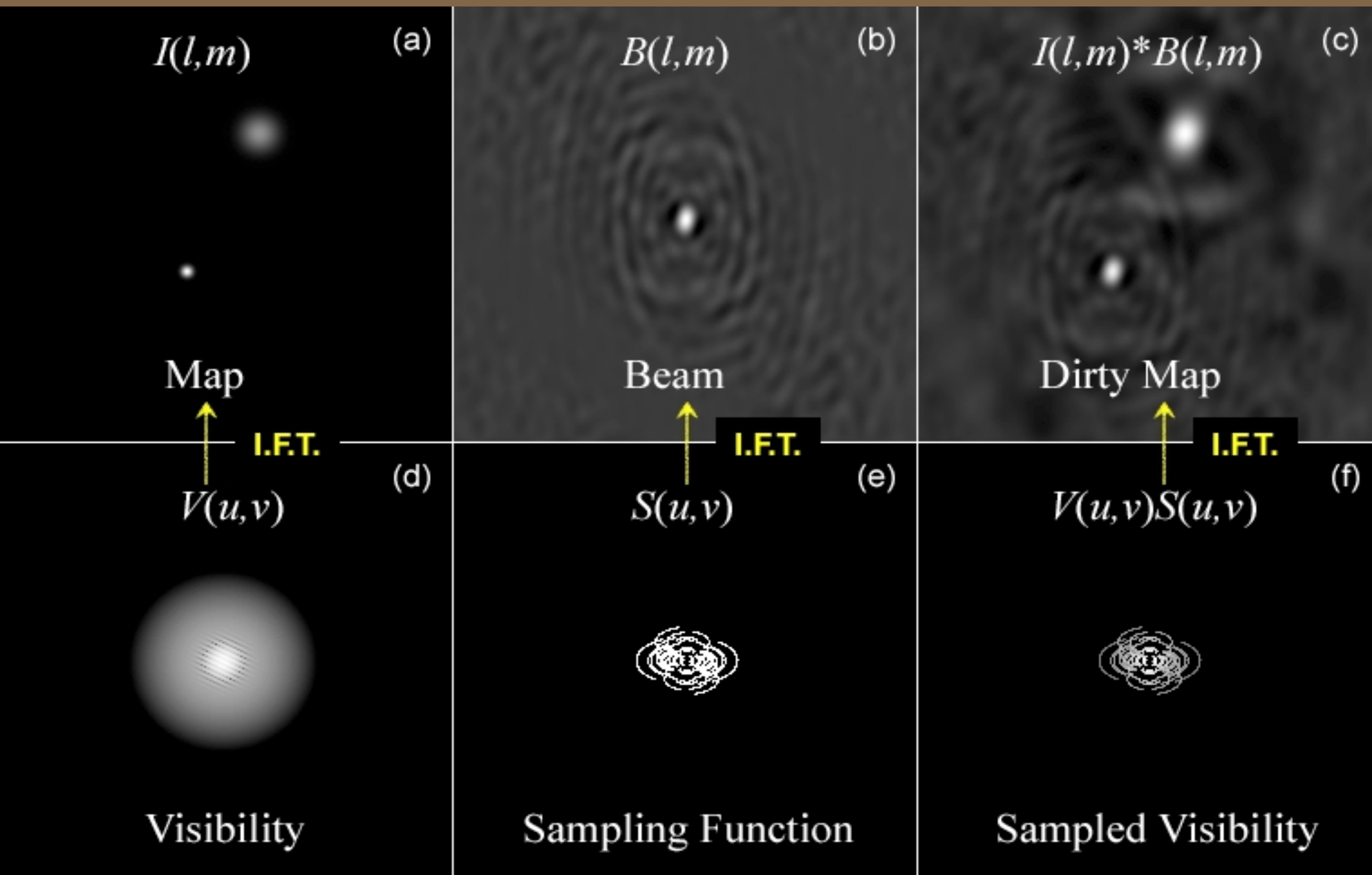
13-02-2014

Radio Measurements

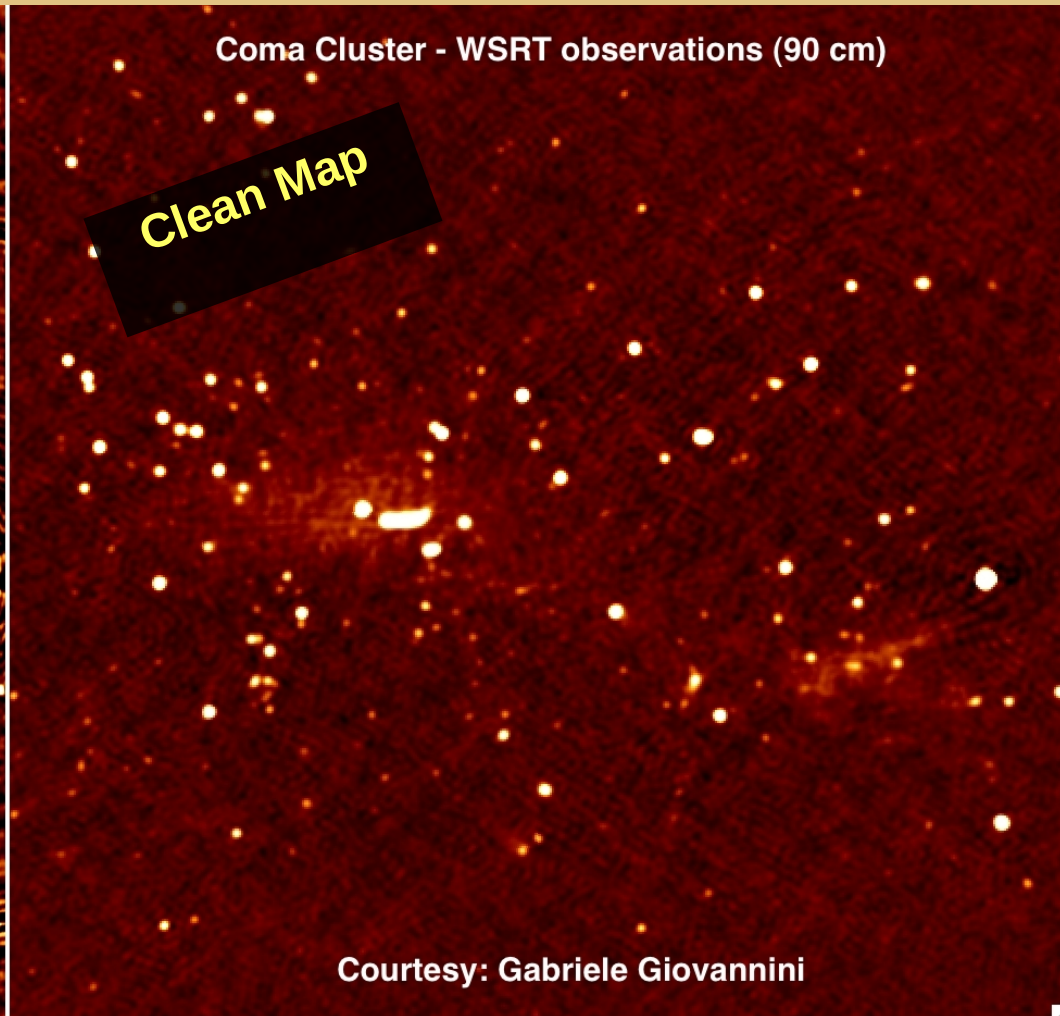
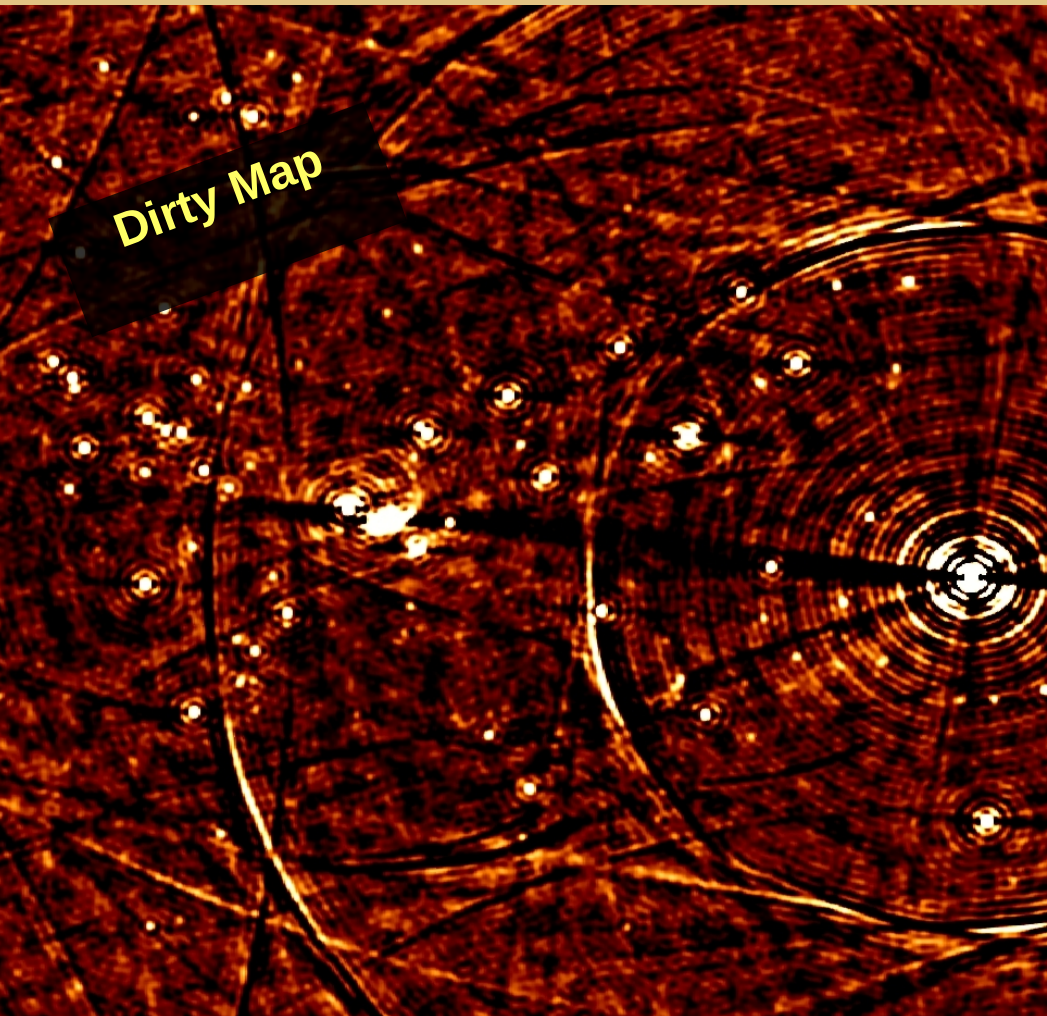


$$V = \langle \vec{E}_1, \vec{E}_2 \rangle$$

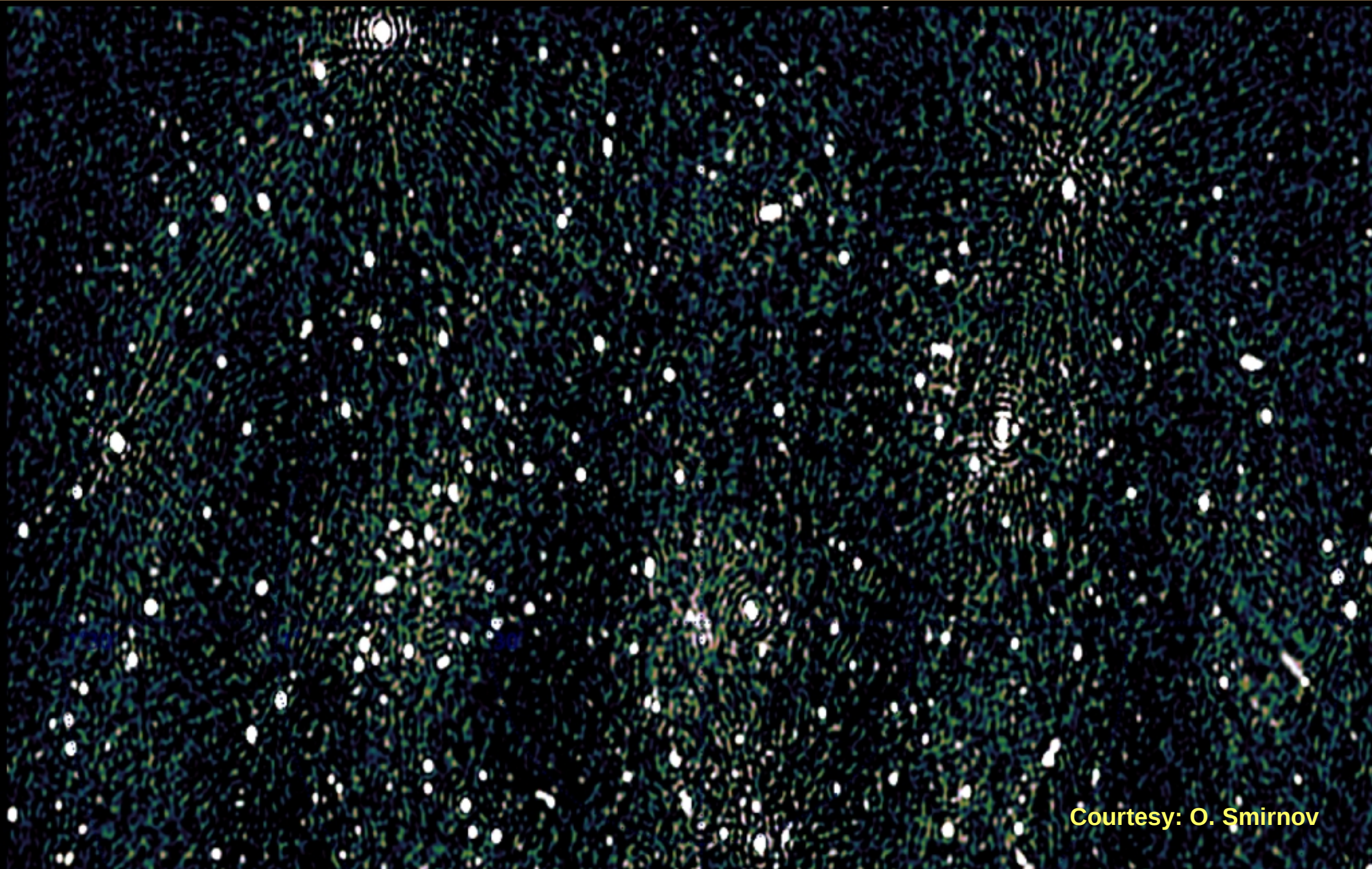
Radio Data



Radio Data: Galaxy Clusters



Deconvolution issues

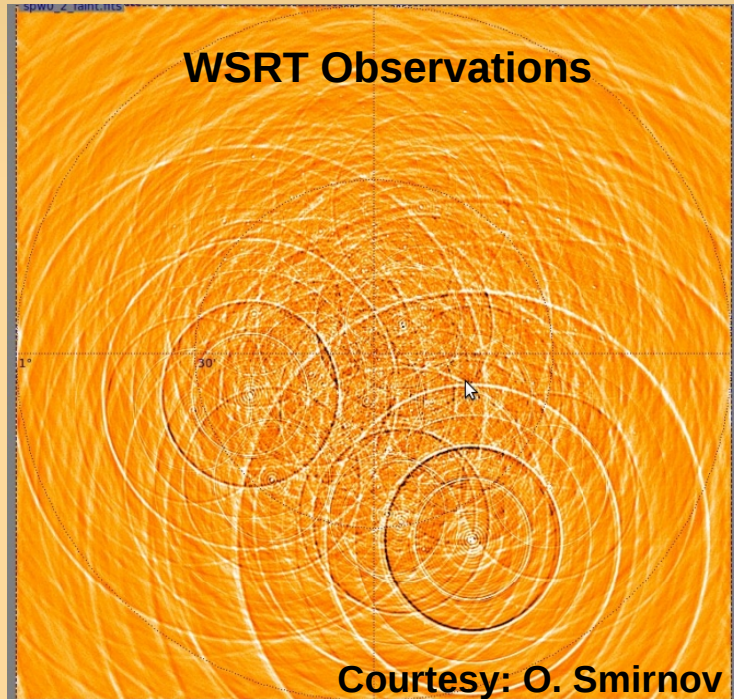


Courtesy: O. Smirnov

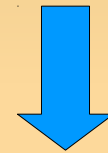
Radio Interferometric Problem

Radio Interferometric model (1D)

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n}, \quad \mathbf{n} \in \mathbb{R}^N$$



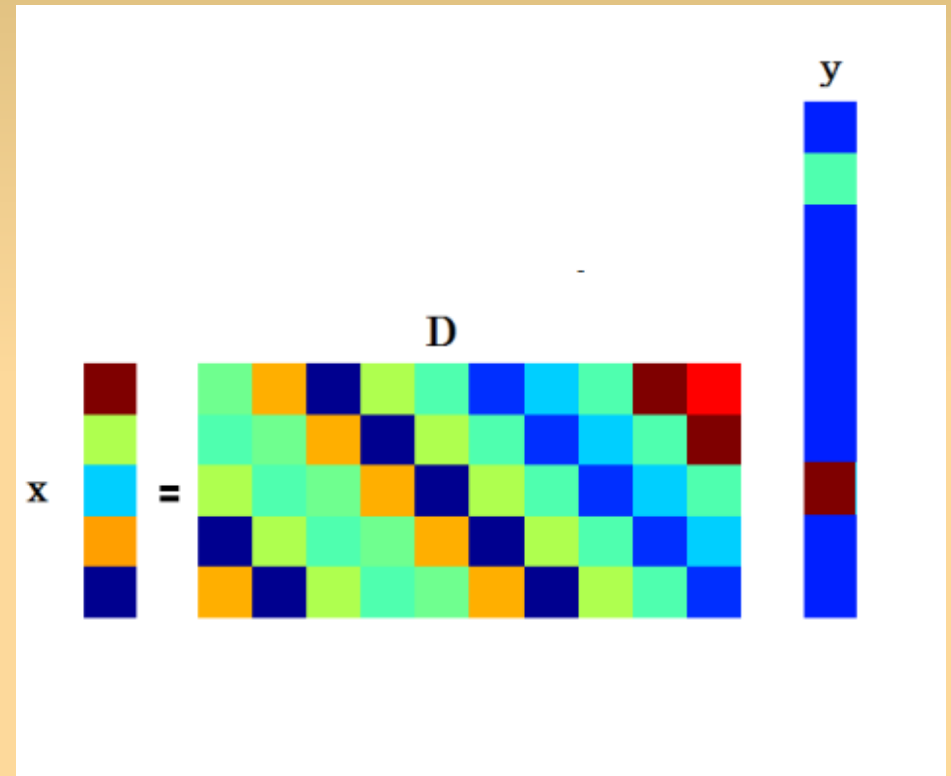
Problem ill posed due to the missing information in the uv coverage



Infinity number of skies that can fit the Dirty map

Sparse Representations

- a **sparse** signal: most of its coefficients equal zero.
- a **dictionary**: a data representation space where the signal can be sparsified.
- an **atom**: a column of a dictionary of the same size as the signal.

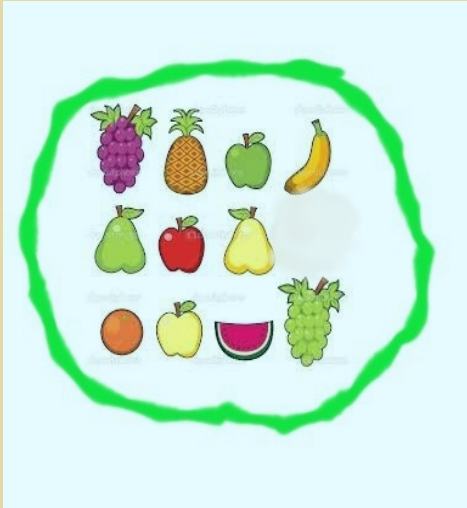


Sparsity Promoting approaches

■ Synthesis Approach

The signal \mathbf{x} is a linear combination of only **few** atoms of a given dictionary \mathbf{S} .

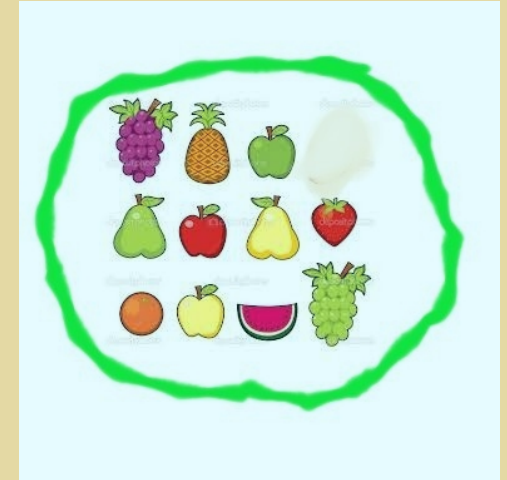
$\mathbf{x} = \mathbf{S}\boldsymbol{\gamma}$, $\boldsymbol{\gamma}$ (*synthesis coefficients vector*) is sparse



■ Analysis Approach

The projection of a signal \mathbf{x} in a given dictionary \mathbf{A} is **sparse**.

$\mathbf{A}^T \mathbf{x} = \mathbf{a}$, \mathbf{a} (*analysis coefficients vector*) is sparse



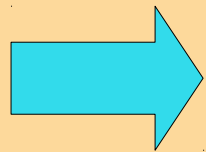
Sparsity Promoting approaches

- **Synthesis Approach**

- + Intuitive design
- Time consuming

- **Analysis Approach**

- + Robust to false detection
- Time consuming



Hybrid approach : iterative analysis then synthesis of the signal by **packets** of atoms in a greedy manner

The Model

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n} = \mathbf{H}\mathbf{X}\mathbf{1}_P + \mathbf{n}, \text{ with } \mathbf{X}_i \geq \mathbf{0}, \forall i \text{ and } P \ll N,$$

sparse synthesis problem with **unknown** atoms.

Analysis by Synthesis Approach

iteration i

Analyze data \mathbf{r}_i with
IUWT-analysis Dictionary

Identify the analysis **sparse** vector
 $\boldsymbol{\alpha}_i$ corresponding to the brightest
sources \mathbf{X}_i in the data

Analysis Step

Estimate the atom \mathbf{X}_i from $\boldsymbol{\alpha}_i$

$$\hat{\mathbf{X}}_i = \arg \min_{\mathbf{z}} \|\boldsymbol{\alpha}_i - \mathcal{P}_{\alpha_i}(\mathbf{A}^T \mathbf{H} \mathbf{z})\|_2^2$$

Add \mathbf{X}_i to the synthesis dictionary \mathbf{X}

$$\mathbf{x} = \sum_{i=1}^P \mathbf{X}_i = \mathbf{X} \mathbf{1}_P$$

Synthesis Step

Remove the contribution of \mathbf{X}_i from
the residual data \mathbf{r}_i

$$\mathbf{r}_{i+1} = \mathbf{r}_i - \gamma \mathbf{H} \hat{\mathbf{X}}_i$$

Simulations & Results

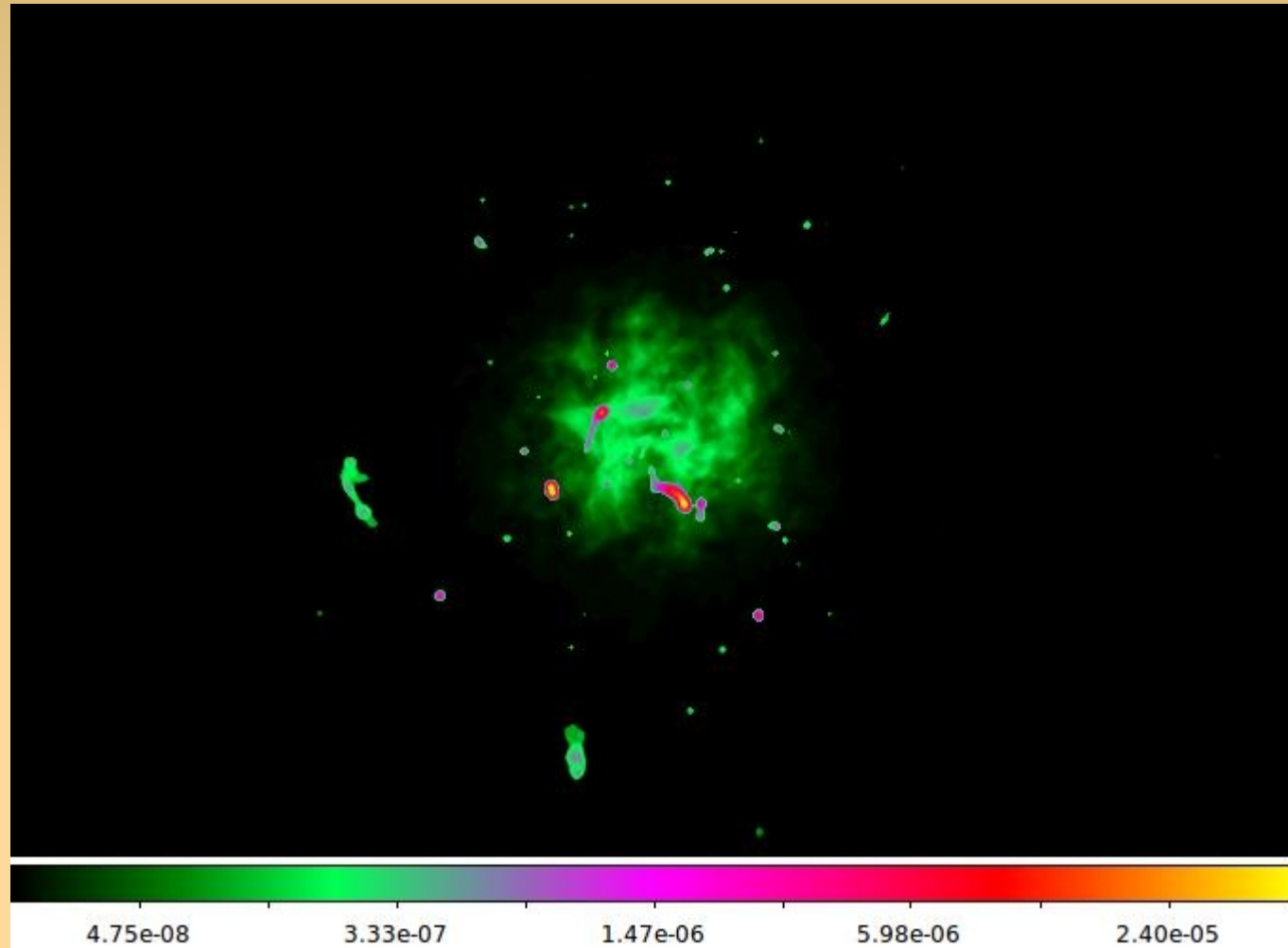


- Simulations using MeqTrees software by (O. Smirnov)



- Simulations of 2h & 8h MeerKat observations

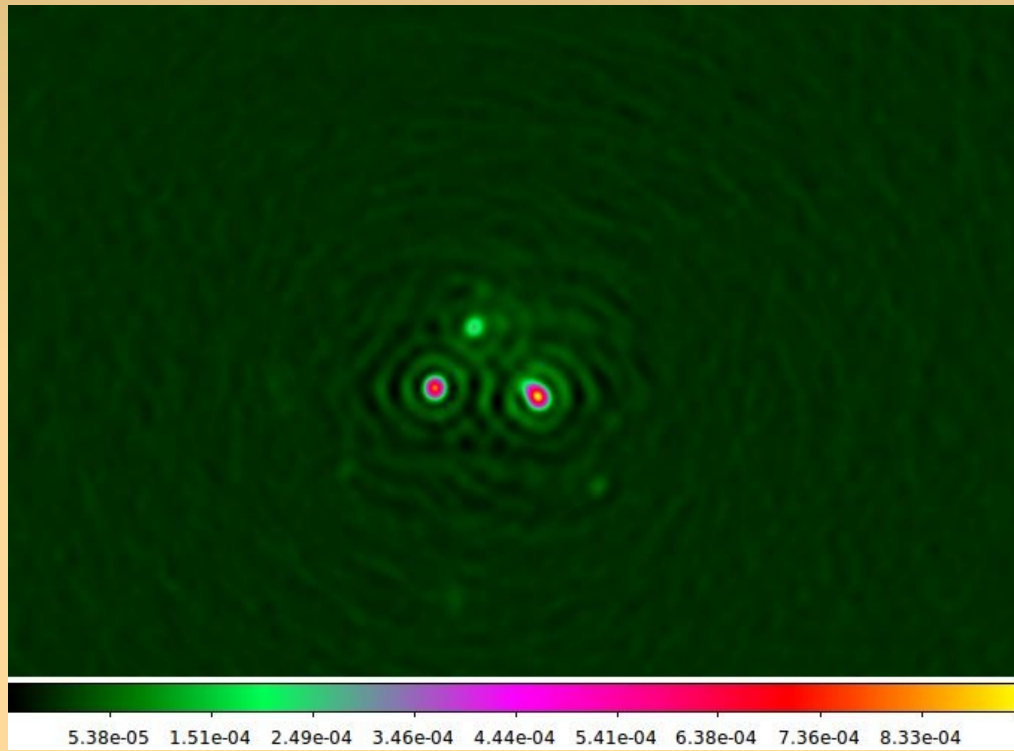
Simulations & Results



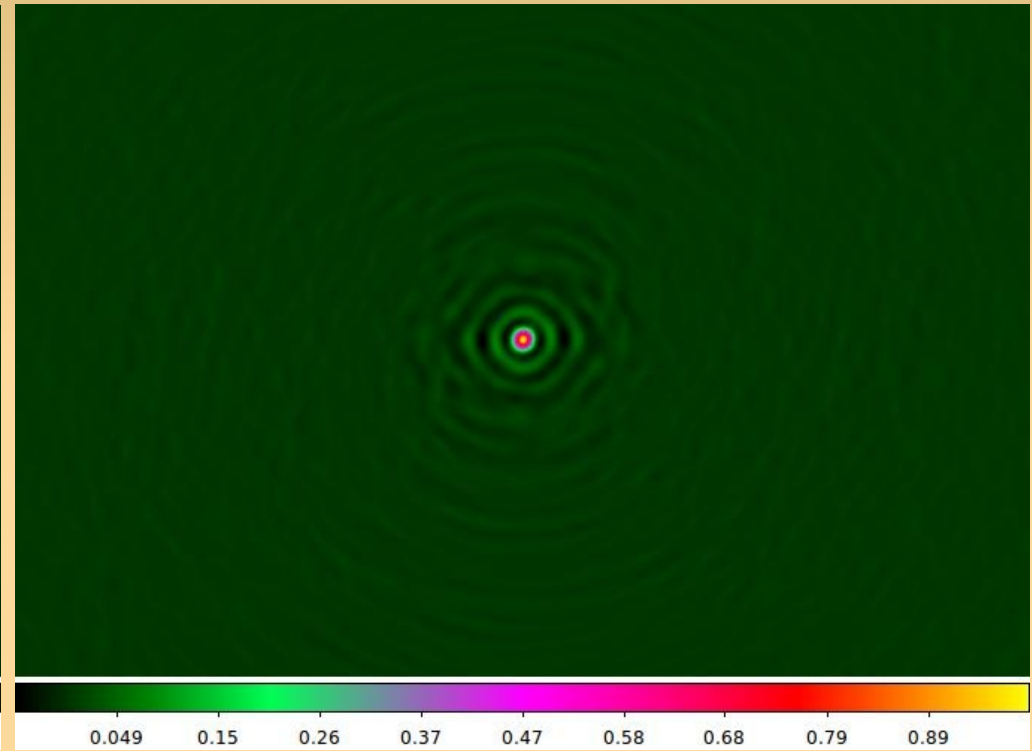
SKY: simulated galaxy cluster

Simulations & Results

MeerKat, 8h Observations



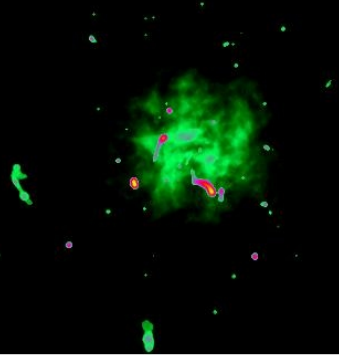
Dirty Map



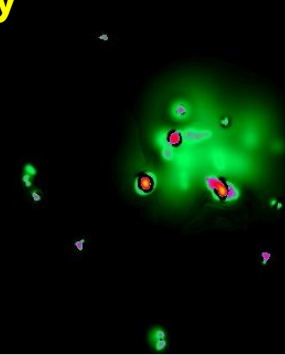
PSF

Simulations & Results

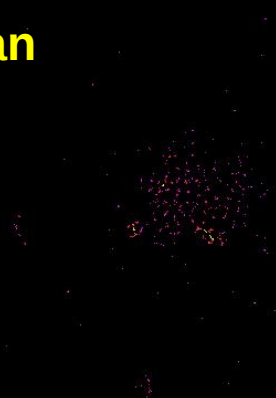
Sky



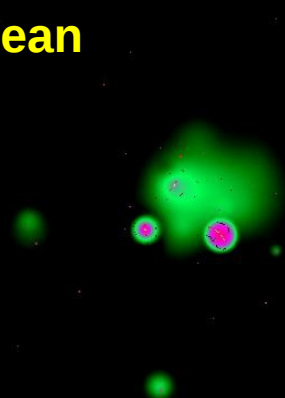
Estimated Sky



Hogbom Clean



Multiscale Clean



5.25e-08

1.47e-07

3.38e-07

7.16e-07

1.48e-06

2.98e-06

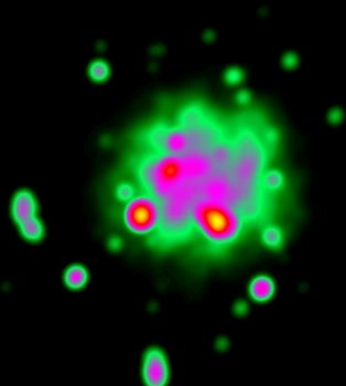
5.99e-06

1.20e-05

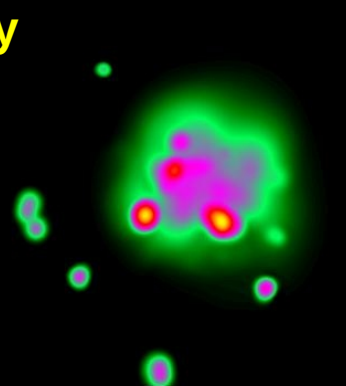
2.40e-05

Simulations & Results

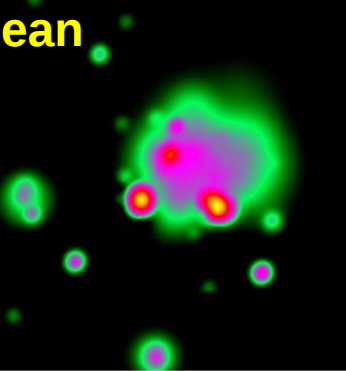
Sky



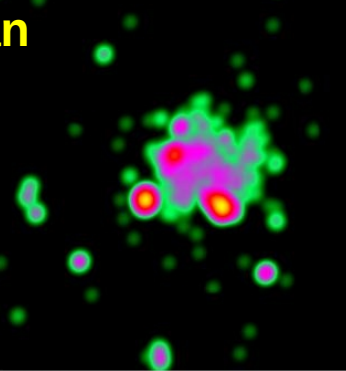
Estimated Sky



Multiscale Clean



Hogbom Clean



1.02e-06

2.86e-06

6.57e-06

1.39e-05

2.87e-05

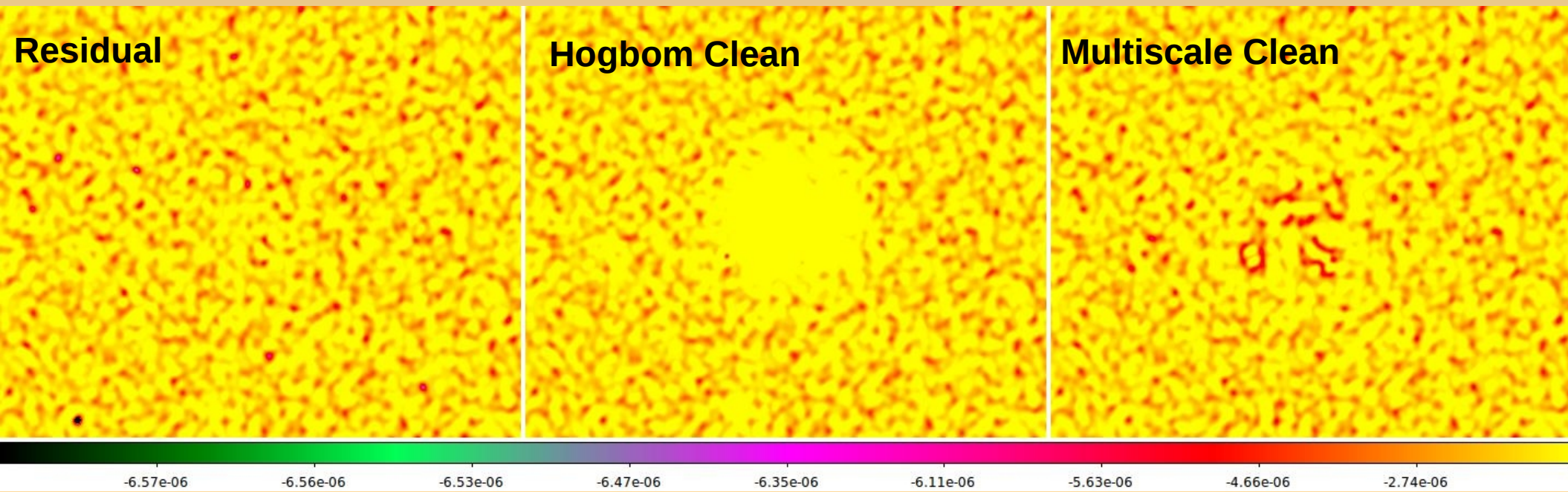
5.80e-05

1.16e-04

2.34e-04

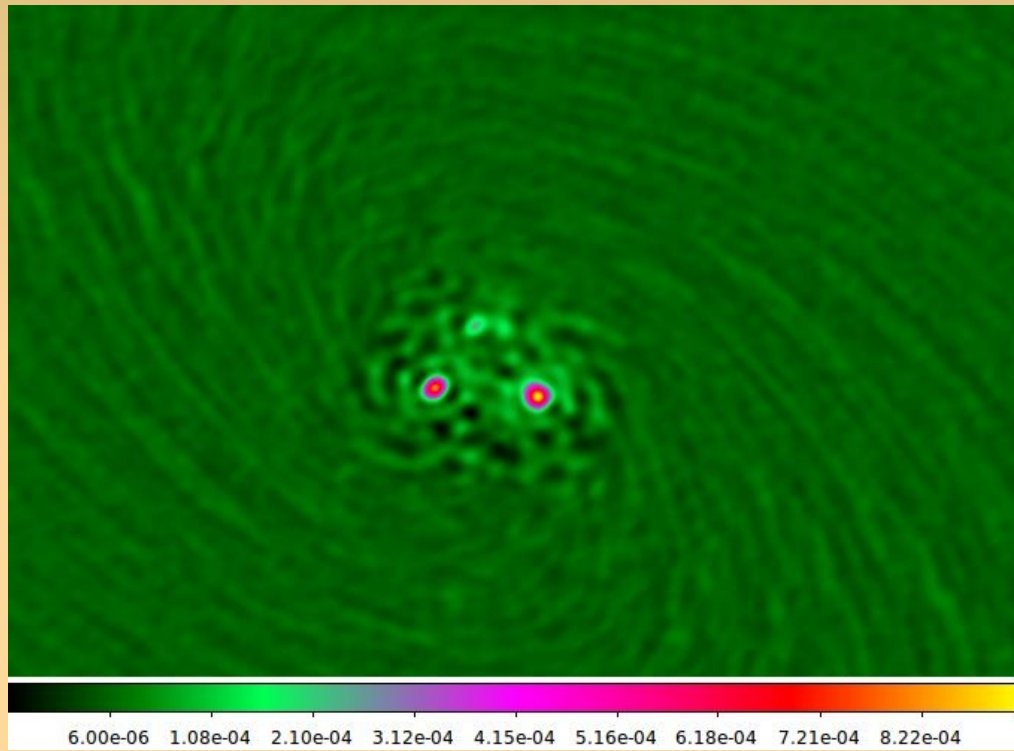
4.66e-04

Simulations & Results

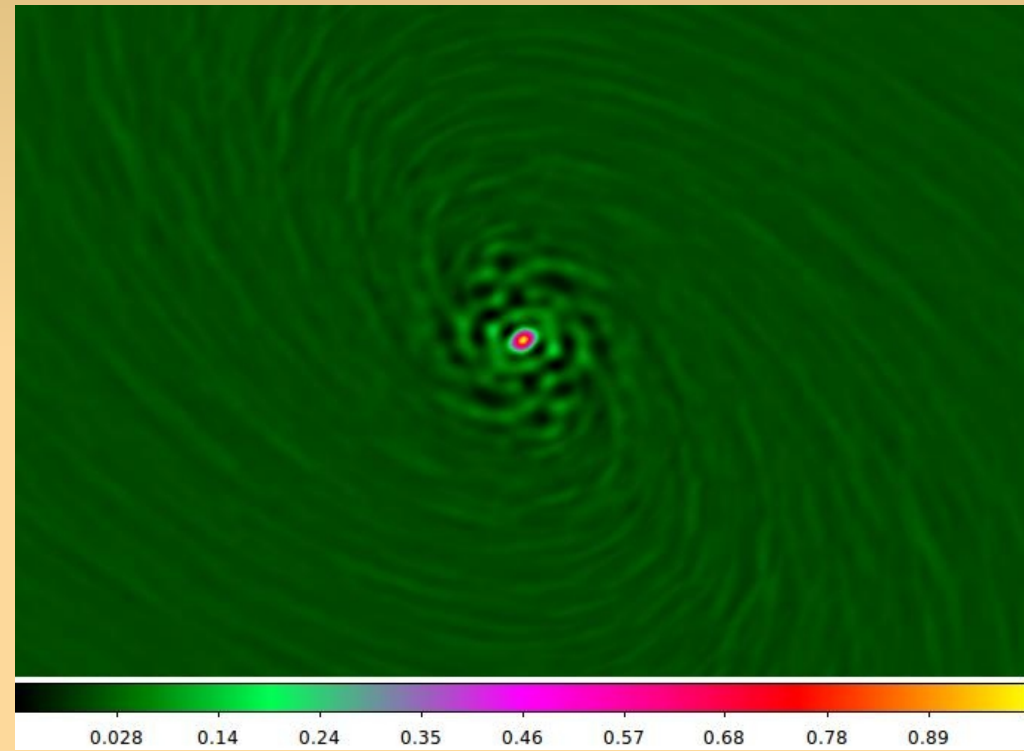


Simulations & Results

MeerKat, 2h Observations



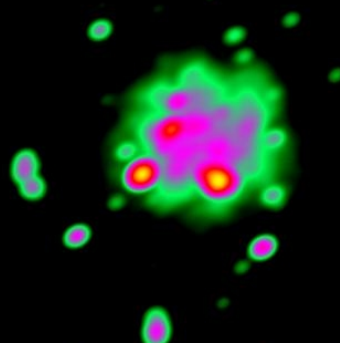
Dirty Map



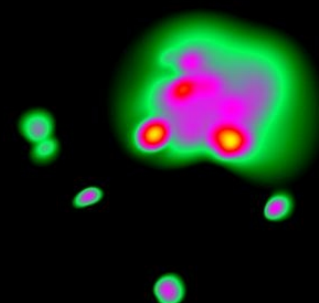
PSF

Simulations & Results

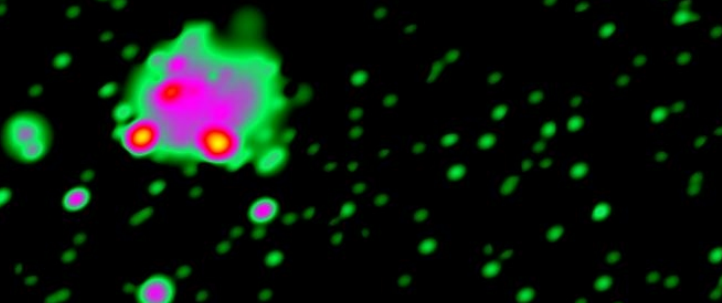
Sky



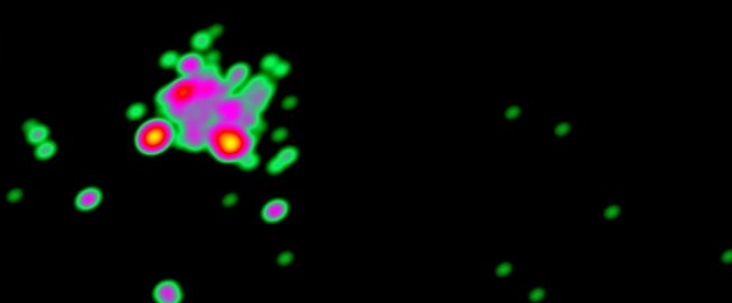
Estimated Sky



Multiscale Clean



Hogbom Clean



1.40e-06

3.20e-06

6.83e-06

1.40e-05

2.85e-05

5.72e-05

1.14e-04

2.30e-04

4.57e-04

Conclusions

- Results are promising!

Very good recovery of both compact and extended sources on realistic simulations & on real data (VLA, Kat7) as well

- On going work

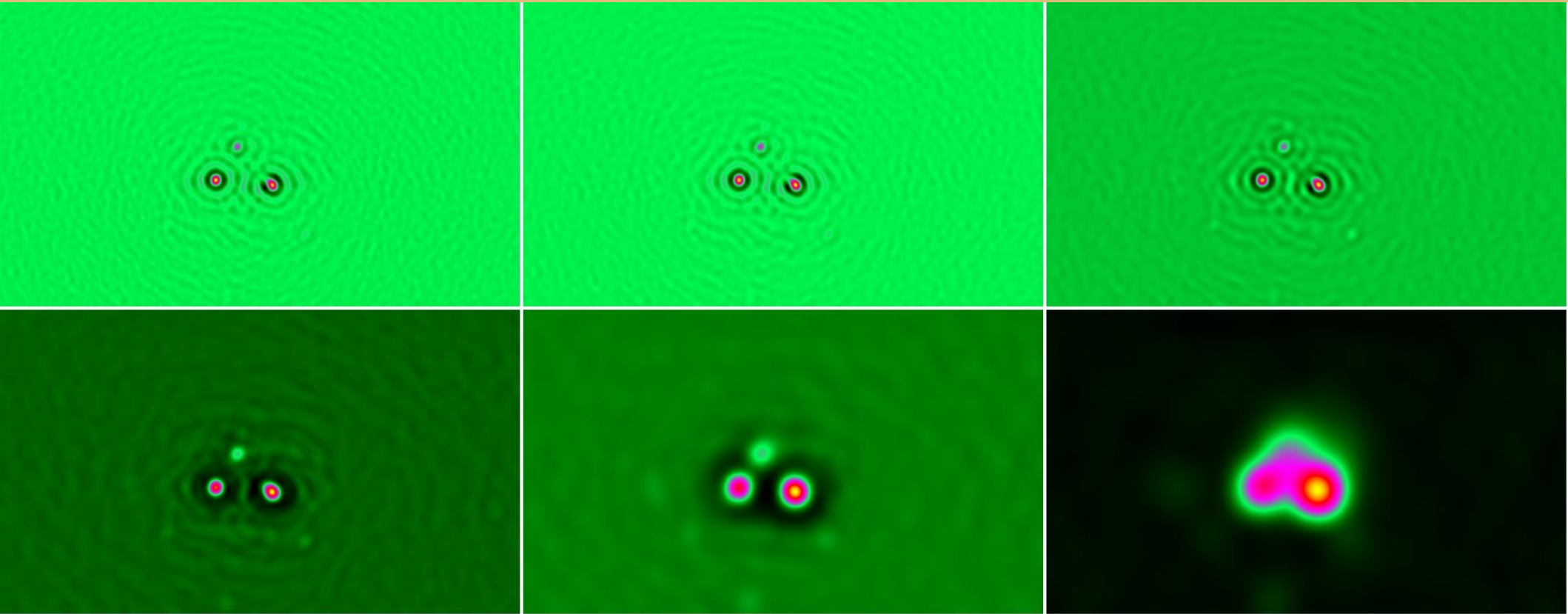
Taking into account the variation of the PSF in the field of view

Source catalog as output of the code

Thanks!



IUWT-analysis vector



Thanks!



Thanks!

